

12. Übungsblatt

Vorlesung Approximationsalgorithmen (Winter 2015/16)

Aufgabe 1 – MAX-SAT

- a) Show that the following algorithm is a $1/2$ -approximation for MAX-SAT. Let τ be an arbitrary truth assignment and τ' be its complement, that is, a variable is true in τ if and only if it is false in τ' . Compute the weight of clauses satisfied by τ and by τ' , then output the better assignment. **3 Punkte**

In the following, let a k -CNF-SAT instance denote a formula in conjunctive normal form, where each clause contains exactly k literals and every variable occurs at most once per clause.

- b) Show that every 3-CNF-SAT instance on at most 7 clauses is satisfiable. **1 Punkt**
- c) Recall the algorithm that just outputs a uniformly random truth assignment. It runs in polynomial time and we proved a lowerbound on the expected weight of the satisfied clauses. We then derandomised this algorithm. This makes the algorithm slower and more complicated. Consider instead the following algorithm for MAX-3-CNF-SAT: keep guessing truth assignments until you find one that satisfies $7/8$ of the clauses. Show that this algorithm runs in expected polynomial time. Compare the advantages and disadvantages of these three algorithms for MAX-3-CNF-SAT. **7 Punkte**
- d) Recall the MAXCUT problem: find a set $S \subseteq V$ such that the number of edges between S and its complement is as large as possible. Solve MAXCUT using MAX-2-CNF-SAT. **5 Punkte**